

2006 Mathematics

Standard Grade General

Finalised Marking Instructions

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Special Instructions

The main principle in marking scripts is to give credit for the skills which have been demonstrated. Failure to have the correct method may not preclude a pupil gaining credit for the calculations involved or for the communication of the answer.

Care should be taken to ensure that the mark for any question or part question is entered in the correct column, as indicated by the horizontal line.

Where a candidate has scored zero marks for any question attempted, "0" should be shown against the answer in the appropriate column.

It is of great importance that the utmost care should be exercised in adding up the marks. Where appropriate, all summations for totals and grand totals must be carefully checked.

- The answer to one part, correct **or incorrect** must be accepted as a basis for subsequent dependent parts of a question. Full marks in the dependent part is possible if it is of equivalent difficulty.
- 3 Do not penalise insignificant errors. An insignificant error is one which is significantly below the level of attainment being assessed.
 - eg An error in the calculation of 16 + 15 would not be penalised at Credit Level.
- Working after a correct answer should **only** be taken into account if it provides **firm** evidence that the requirements of the question have not been met.
- In certain cases an error will ease subsequent working. **Full** credit cannot be given for this subsequent work but **partial** credit may be given.
- Accept answers arrived at by inspection or mentally, where it is possible for the answer to have been so obtained.
- 7 Do not penalise omission or misuse of units unless marks have been specifically allocated to units.

A wrong answer without working receives no credit unless specifically mentioned in the marking scheme.

The rubric on the outside of the Papers emphasises that working must be shown. In general markers will only be able to give credit to partial answers if working is shown. However there may be a few questions where partially correct answers unsupported by working can still be given some credit. Any such instances will be stated in the marking scheme.

Acceptable alternative methods of solution can only be given the marks specified, ie a more sophisticated method cannot be given more marks.

Note that for some questions a method will be specified.

- In general do not penalise the same error twice in the one question.
- 11 Accept legitimate variations in numerical/algebraic questions.
- Do not penalise bad form eg $\sin x^0 = 0.5 = 30^0$.
- A transcription error is not normally penalised except where the question has been simplified as a result.

Mathematics Standard Grade – General Level 2006 – Paper 1

Marking Instructions

Award marks in whole numbers only

Question No			Illu	strations of evidence each mark	for awarding
1 (a)	Ans:	1 · 93			
	•1	Correct addition followed by correct subtraction	•1	1.93	1K
(b)	Ans:	91 000			
	•1	Correctly multiply 13 by 7000	•1	91 000	1K
(c)	Ans:	0 · 113			
	•1	Correctly divide 56 · 5 by 500	•1	0 · 113	1K
(d)	Ans:	27 · 6 (litres)			
	•1	Correct division	•1	9 · 2	
	•2	Correct multiplication	•2	27 · 6 (litres)	2K
					2K

Notes:

In part (d)

(i) Correct divisions are by 10 (leading to 9.2) or by 100 (leading to 0.92).

(ii)	Final answers	with working	without working
	27.6	2/2	2/2
	2.76 (3%)	1/2	0/2
	$30\frac{2}{3}$, 30.6 (92 ÷ 3)	1/2	0/2

Question No			Give 1 mark for each		Illustrations of evidence for awarding each mark			ding
2		Ans:	(£) 5 · 66					
		•1	Correctly divide 8 · 49 by 3	•1		2 · 83		
		•2	Subtract above answer from 8 · 49	•2		$8 \cdot 49 - 2 \cdot 83$		
		•3	Correct subtraction	•3		(£) 5 · 66		3K
Notes	:							
	(i) A	Alternative s	strategy					
	•	¹ Correctly	divide 8·49 by 3	2	2.83			
	•	² Multiply	above answer by 2	: 2	2.83	x 2		
	•	³ Correct n	nultiplication •3	((£)5·66			
	5 5	Final answer 6-66 6-69 (using 0 6-94 (using 0	3/3 ·33) 2/3			witho	2/3 1/3 1/3	
3		A	(0) 2 2108					
3		Ans:	$(\$) \ 3 \cdot 2 \times 10^8$	n •1		220 000 000		
		•1	Correct numerical representatio	n		320 000 000		
		•2	Correct scientific notation	•2		$(\$) 3 \cdot 2 \times 10^8$		2K
Notes	:							
	(i) F	For correct fi	nal answer of 3·2 x 10 ⁸ with or w	ithout v	vorl	king – award 2/2.		
		Solutions 320 000 000	with/without wor 1/2	king				
	3	320 x 1 000 0 32 x 10 ⁷ 320 x 10 ⁶	1/2 1/2 1/2					
		3.20×10^{2}	$1/\mathcal{L}$					

Question No			Give 1 mark for each		Illustrations of evidence for awarding each mark		
4	(a)	Ans:	1 2 3 4 5 5 8 14 17				
		•1	No. of dots for 1 and 2 stars	•1	5, 8		
		•2	No. of dots for 4 and 5 stars	•2	14, 17 2R		
	(b)	Ans:	d=3s+2				
		•1&2	Correct formula	•1&2	d = 3s + 2 2R		
	(c) (i)	Ans:	30				
		•1	Correctly dividing 300 by 10	•1	30 1R		
	(ii)	Ans:	92				
		•1	Correct strategy	•1	$3 \times 30 + 2$		
		•2	Correct calculation	•2	92 2R		

In part (b)

- (i) For an answer of (=) 3s + 2 award 1/2.
- (ii) Do not penalise bad form eg d = 2s + 2 + s.
- (iii) A formula in words is not acceptable.
- (iv) For s = 3d + 2 award 0/2.

In part (c) (ii)

- (i) Solution may be obtained by extending table.
- (ii) For a correct final answer of 92 without working award 2/2.

Question No		Give 1 mark for each	Illus	strations of evidence for awarding each mark
5	Ans:	$-\frac{3}{8}$		
	•1	Evidence of 3 and 8	•1	3 and 8
	•2	Correctly forming gradient	•2	$-\frac{3}{8}$
				2K

For a final answer of $-\frac{3}{8}$ without working – award 2/2.

6 (a)	Ans:	$\frac{3}{10}$			
	•1	Correctly finding P(blue)	•1	$\frac{3}{10}$	1K
(b)	Ans:	$\frac{2}{7}$			TK.
	•1	Correct subtraction to find number of balls in box	•1	10 - 3 = 7	
	•2	Calculating P(green)	•2	$\frac{2}{7}$	
					2R

Notes:

In part (b)

- (i) For a final answer of $\frac{2}{7}$ without working award 2/2.
- (ii) Accept variations in language eg 2 out of 7, 2-7, 2 to 7, 2:7.

Question No	Give 1 mark for each	Illustrations of evidence for awarding each mark		
7 (a)	Ans: $3\frac{1}{2}$ (hours) • Finding time difference	• 1 8am to 11:30 am = $3\frac{1}{2}$ (hours)		
(b)	Ans: $9\frac{1}{2}$ (hours)			
	•¹ Finding 2 more time differences	• 1 Two from 2, $2\frac{1}{2}$, $1\frac{1}{2}$		
	• Finding remaining time difference	• Remaining time difference		
	• Correctly adding times to answer in (a)	\bullet ³ $9\frac{1}{2}$ (hours)		
Notes:				
In part (a) Allo	$w \pm 5$ min on reading from graph.			
8 7	ll answers with working $(3\frac{1}{2} + 2 + 2\frac{1}{2} + 1\frac{1}{2})$ 3/3 $(3\frac{1}{2} + 2 + 2\frac{1}{2})$ 2/3 $(3\frac{1}{2} + 2 + 1\frac{1}{2})$ 2/3 $(3\frac{1}{2} + 2 + 1\frac{1}{2})$ 2/3 $(2 + 2\frac{1}{2} + 1\frac{1}{2})$ 2/3 $(2 + 2\frac{1}{2} + 1\frac{1}{2})$ 2/3	without working 2/3 0/3 0/3 0/3 0/3 0/3		
8 (a)	Ans: 1 0 5 2 3 5 5 8 3 0 2 3 4 5 8 4 1 2 4 6 5 2 5 6 2 (n=19 1 5=15) • Stem correct • All leaves on correct level • Leaves ordered correctly Ans: 34	•¹ •² •³		
ζ=1	•¹ Median correctly identified	•¹ 34		

Question No	Give 1 mark for each		Illustrations of evidence for awarding each mark		
9	Ans:	14°			
	•1	Knowing ∠OLM is right angled	•1	∠OLM = 90°	
	•2	Knowing how to find ∠LOK	•2	$180 - 2 \times 52 \ (= 76^{\circ})$	
	•3	∠LMO calculated correctly	•3	$180 - (90 + 76) = 14^{\circ}$	3R
Notes:			1		

(i) Alternative strategy

1 Knowing \angle OLM is right angled • 90

2 Knowing how to find \angle KLM and \angle LKM • 90 – 52 (= 38°), 180 – 52 (= 128°)

 \angle LMO calculated correctly \bullet^3 180 – (38 + 128) = 14°

(ii)	Final answers	vith working	without working
	14	3/3	2/3
	38 (from \angle LOK = 52°)	2/3	0/3
	26 (from \angle LOK and/or \angle KLO = 64°) 2/3	0/3
	7 (from \angle LOK = 83°)	2/3	0/3

(iii) Angles correctly marked on diagram may be accepted.

KU 17 marks RE 16 marks

[END OF PAPER 1 MARKING INSTRUCTIONS]

Mathematics Standard Grade – General Level 2006 – Paper 2

Marking Instructions

Award marks in whole numbers only

Question No	Give 1 mark for each		Illustrations of evidence for awarding each mark	
1	Ans:	(£) 1185		
	•1	Find correct cost of 7 nights		•¹ 825
	•2	Calculate cost of 5 extra night	S	$\bullet^2 \qquad 5 \times 72 = 360$
	•3	Correct addition of above		\bullet ³ 825 + 360 = 1185
Note: For a final answer of 864 (12 x 72) with working – award 1/3				
2	Ans:	270 pages		
	•1	Divide 63 by 7		\bullet^1 63 ÷ 7
	•2	Multiply above answer by 30		\bullet^2 9×30
	•3	Calculations correct		• ³ 270
Notes:				
(i) Calo	culations	must include multiplication and	divis	ision.
(ii) For	a final an	swer of 252 (28 minutes) or 315	(35	5 minutes) with working – award 1/3
(iii) Alte	ernative s	strategy		
•1	\bullet^1 Divide 30 by 7 \bullet^1		1	30 ÷ 7
•2	Multiply	above answer by 63	2	4·29 x 63
•3	Calculati	ons correct	3	270 (·27)

Question No		Give 1 mark for each Illustrations of evidence for awar each mark	ding
3	Ans:	6 0 0 0 30 5 1 0 0 28 5 0 1 0 27 5 0 0 1 25 4 1 1 0 0 25 For one correct row For a second correct row For a third correct row	
	•4	For two final rows correct	4R
Comment:	Scrip	se mark according to marking instructions ots from centres where the Chief Invigilator has reported that the Correction ce had not been read out will be actioned by the PA prior to certification.	1
4	Ans:	176 · 1 (cm)	
	•1	Valid trig ratio	
	•2	Correct rearranging $e^2 d = 180 \times \cos 12^\circ$	
	•3	Correct calculation involving trig ratio $d = 176 \cdot 06657 \dots$	
	•4	Correct rounding \bullet^4 $d = 176 \cdot 1 \text{ (cm)}$	4K

- (i) Final mark is for correct rounding following a calculation
- (ii) Credit should be given where a more laborious method is used

(iii)	Final answers	with working	without working
	176·1	4/4	3/4
	151·9 [RAD]	4/4	3/4
	176·8 [GRAD]	4/4	3/4
	$37.4 (180 \times \sin 12)$	3/4	0/4
	38·3 (180×tan 12)	3/4	0/4

Question No	Give 1 mark for each		Illustrations of evidence for awardi each mark	
5	Ans:	12 (hours)		
	•1	Knowing how to calculate basic pay	•1	$54 \times 5 \cdot 6 (= 302 \cdot 4)$
	•2	Knowing to subtract to find O/T pay	•2	$436 \cdot 8 - 302 \cdot 4 (= 134 \cdot 4)$
	•3	Knowing how to calculate O/T rate	•3	$5 \cdot 6 \times 2 (= 11 \cdot 2)$
	•4	Knowing to divide O/T pay by O/T rate to find number of hours and all calculations correct (min. 2, must involve a division)	•4	$134 \cdot 4 \div 11 \cdot 20 = 12 \text{ (hours)}$ 4R
Notes:		·		4K

(i) Alternative strategy

- •¹ Knowing how to calculate total no. of hours worked.
- \bullet^1 436·80 ÷ 5·60 (= 78)

• ² Knowing to subtract 54 from above

 \bullet^2 78 – 54 (= 24)

• ³ Knowing to divide above by 2

- \bullet^3 24 ÷ 2
- All calculations correct, (min 2, must involve a division) = 12 (hours)
- (ii) For a final answer of 12 (hours) without working award 2/4

6 (a)	A	Ans:	3(2a+5b)			
	•	1	Finding highest common factor	•1	3	
	•	2	Correct factorisation	•2	(2a+5b)	2K
(b)	A	Ans:	<i>x</i> = 8			2K
	•	1	x terms gathered	$ullet^1$	3x	
	•	2	Number terms gathered	•2	24	
	•	3	Correct solution	•3	<i>x</i> = 8	3K
						JK

Note:

In part (b) for x = 8 without working – award 0/3.

Questio No	on	Give 1 mark for each	II	Illustrations of evidence for awarding each mark		
7	Ans:	10 (min)				
	•1	Knowing to use formula to find time	•1	$T = 80 \div 60$		
	•2	Correct time calculation	•2	= 1 · 3		
	•3	Knowing to change above answe into hours and minutes	$r \mid \bullet^3$	1 hr 20 min		
	•4	Correct time difference	•4	10 (min) 4F		
Notes:			<u> </u>			
(i)	Alternative	strategy				
	•¹ Valid str	ategy \bullet^1 60 km	1	hr		
	• Correct t	ime calculation • ² 20 km	2	20 min		
	• ³ Correct i	ourney time \bullet^3 1 hr 2	0 min			
		,				
		ime difference \bullet^4 10 (m				
(ii)	Final answer	rs with works	ng	without working 3/4		
	10 (min) 0·166 (hr)	4/4 4/4		3/4		
	0·17 (hr) (1·5			2/4		
	\ / \	cleading to 1 hr 18 min) 3/4		2/4		
		·33 leading to 1 hr 19·8 min) 3/4		2/4		
		leading to 1 hr 33 min) 3/4		0/4		
	45 (min) (60	÷ 80 leading to 45 min) 3/4		0/4		
8	Ans:	20·7 (m)				
	•1	Correct use of Pythagoras' Theorem	•1	$4\cdot 3^2 + 2\cdot 9^2$		
	•2	Correct Pythagoras calculation	•2	26.9		
	•3	Correct square root of above	•3	5·18		
	•4	Correct multiplication of above by 4	•4	$P = 20 \cdot 7 \text{ (m)}$		

For a final answer of 20·7 or 20·8 (4×5 ·2) without working – award 3/4

(Question No		Give 1 mark for each	Illu	strations of evidence for awar each mark	ding
9	(a)	Ans:	0 · 442			
		•1	Calculating area of $\frac{1}{4}$ circle	•1	$\frac{1}{4} \times \pi \times 0 \cdot 75^2$	
		•2	Correct calculation involving π	•2	0 · 4	2K
	(b)	Ans:	twice			210
		•1	Knowing to calculate no. of times desk can be painted	•1	<u>1</u> 0 · 4	
		•2	Interpreting answer correctly	•2	twice	2R

In parts (a) and (b) for a correct final answer without working – award 2/2

In part (a) for a final answer of 1.7... with or without working – award 1/2

In part (b) (i) The final answer must be a whole number

(ii) Any valid comparison can lead to an award of 2/2

Question No	Give 1 mark for each		Illustrations of evidence for awarding each mark		
10 (a)	Ans:	(£) 114			
	•1	Correct information chosen from table	•1	28 and 15	
	•2	Correct calculation	•2	$3 \times 28 + 2 \times 15 = (£) 114$	2K
(b)	Ans:	No, it will cost her £6 more			
	•1	Knowing to calculate the number of hours Maria is at nursery	•1	$3 \times 6 + 2 \times 3 = 24 \text{ hours}$	
	•2	Knowing to multiply no. of hours by 5 and calculations correct	•2	$24 \times 5 = £120$	
	•3	Compares cost with answer to (a)	•3	No 120 > 114 ie £6 more per week	
					3R

In part (a) For a correct final answer without working – award 2/2

In part (b)

- (i) For correct reason involving correct comparison without further working award 3/3
- (ii) Alternative strategy
 - •¹ Calculating the cost of $\frac{1}{2}$ days and full days •¹ 15 and 30
 - Comparing the cost of $\frac{1}{2}$ days 15 = 15, ie cost is same
 - Comparing the cost of full days 30 > 28, ie £2 more per full day

Question No		Give 1 mark for each	Illustrations of evidence for awarding each mark
11	Ans:	Position of ship shown	
	•1	Draws line on bearing 110° from Lossiemouth correctly	•¹ 110°
	•2	Draws line on bearing 075° from Leuchars correctly	•² 75°
	•3	Extends lines to show position of ship	• ³ 3R

Note: Allow $\pm 2^{\circ}$ tolerance

No marks can be awarded to candidates who mark a position for the ship without showing construction lines

Question No	1	Give 1 mark for each	Illustrations of evidence for awarding each mark	
12	Ans:	(£) 55·08		
	•1	Knowing to calculate price for a new customer	• $\frac{1}{5}$ of $765 = 153$ 765 - 153 (= 612)	
	•2	Knowing to find 8% of above answer and add to above	$ \bullet^{2} 0 \cdot 08 \times 612 = 48 \cdot 96 \\ 612 + 48 \cdot 96 (= 660.96) $	
	•3	Knowing to find monthly installment	\bullet ³ 660.96 ÷ 12	
	•4	All calculations correct within valid strategy	$\bullet^4 = (£) 55.08$ 4R	
Notes:				
•	_	to find base monthly premium to find monthly premium for new c	$\bullet^{1} 765 \div 12 = 63.75$ ustomer $\bullet^{2} 63.75 \div 5 = 12.75$	
•	³ Knowing	to find 8% of above and add to abo	63.75 - 12.75 = 51 we	
•	⁴ All calcu	lations correct	$\bullet^4 = (£) 55.08$	
1 2	Final answer 55·08 68·85 46·92 13·77 4·08 624·24 165·24	with workin 4/4 3/4 3/4 3/4 3/4 3/4 2/4 2/4	g without working 3/4 0/4 0/4 0/4 0/4 0/4 0/4 0/4	

KU 23 marks RE 24 marks

[END OF MARKING INSTRUCTIONS]

FINAL	KU 40
TOTALS	RE 40